

# 10. Quantum physics

version of October 30, 2003

## Quantum leaps

Question: What do all the following phenomena have in common?

- lasers
- solar cells
- computer circuitry (integrated circuits)
- digital camera imagers
- superconductors

Answer: They all make use of “quantum” phenomena that were discovered in the 20<sup>th</sup> century.

The term “quantum leap” has become a metaphor for anything that changes abruptly. But originally it referred to the behavior of light and of electrons. If you have visible light, then no matter how dim or bright the light is, it will always be absorbed in quantum amounts that are multiples of 2 electron-volts. It was a great surprise to early physicists to discover this fact. Moreover, if the light is blue, the amount is slightly larger than 2 eV, and if it is red, the amount is slightly less than 2 eV. This peculiar behavior was called the “photoelectric effect.” The light that is abruptly absorbed or emitted was given a name: the photon. Bright light does not contain photons with greater energy. It just contains more photons with 2 eV energy.

Electrons also show quantum leaps. When an atom is hit by light, it sometimes makes one of its electrons leap into a different, more energetic orbit. In effect, the atom now contains extra energy. We say that the atom is “excited.” The electron can leap back to the old orbit, but only if it loses the energy it gained. It can do this by emitting a quantum of light, a photon.

## Electron waves inside atoms

We now know that all electrons, protons, indeed all particles, behave in the same quantum manner: when detected, they behave like particles, but in between, they travel like waves.

The electron orbits the nucleus as a wave. It is the negative charge of the electron wave that is attracted to the positive charge of the nucleus. The frequency of this wave is related to the energy of the electron by the same Einstein equation as before:

$$E = hf$$

But since the electron wave moves in circles, it has to be careful not to cancel itself out. That means that only certain values of energy are allowed – those that have frequencies that reinforce after one orbit. The allowed kinetic energies for the hydrogen atom – the electron energies of the waves that circle the atom -- have been measured. They include the following energies: 13.6 eV, 3.4 eV, 1.5 eV, 0.85 eV. We say that these are “allowed” energies. That means that they are the energies that don’t lead to self-cancellation. There are other allowed energies too. They can all be described by a simple formula that was discovered by Niels Bohr:

$$KE = 13.6/n^2$$

where n is an integer (n = 1, 2, 3, ...). Different values of n give the energies in the list. Orbits with other kinetic energies cancel themselves out, and so – in consequence – waves with those energies do not exist in orbits around the hydrogen atom.

That is a truly remarkable consequence of the wave nature of electrons. We say that the energy that the electron is able to have in the hydrogen atom is limited to specific values given by the formula. They can’t have in-between values. There is a special word for this. We say that the allowed energies are *quantized*.

Not all energies are quantized. An electron that is moving through empty space can have any kinetic energy. The quantization of energy came about for the hydrogen atom because the electron was moving in an orbit.

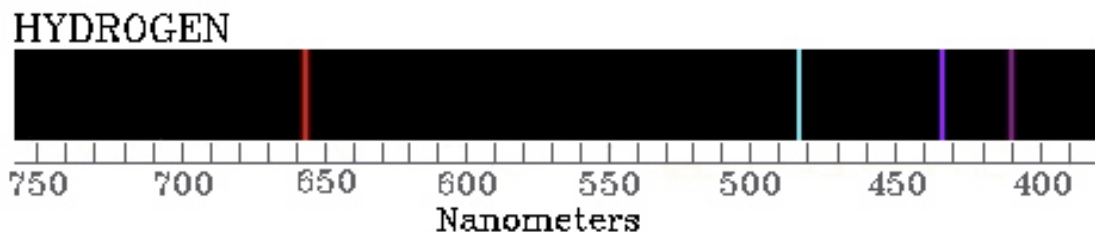
## Photon emission – the fingerprint of the atom

When one hydrogen molecule collides with another (as it does in a gas) it can knock the electron from one allowed orbit to another one that has a greater energy. The electron can lose this energy and fall back into the original orbit by radiating an electromagnetic wave which carries off the energy difference. In our new language of quantum physics, we say that the electron changes its orbit (a quantum jump) and emits a photon. If the energy *difference* between the two orbits is E, then the frequency of the photon is given by the Einstein equation

$$E = hf$$

So the frequency of the emitted light has only certain values – those that correspond to the differences in the quantized energy levels. That means that the color of the emitted light is also quantized. Only certain frequencies are allowed. When we make a rainbow from the emitted light from a large number of hydrogen molecules, not all colors are

present. A picture of the spectrum of the hydrogen atom is shown below. The “Nanometer” scale refers to the wavelength of the light.



(borrowed from <http://www.nhn.ou.edu/~kieran/reuhome/vizqm/figs>)

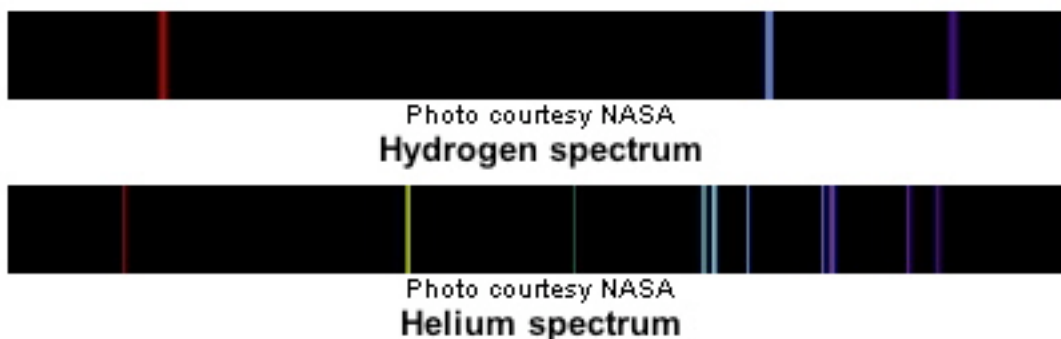
For comparison, the figure below shows the colors of the rainbow – the colors that you get when you shine sunlight (white light) on a prism.



In the both images above, the colors were often spread out in the vertical direction. For the hydrogen case, that made the color appear as lines. For this historic reason the quantized colors are often still referred to as “spectral lines.”

A hot hydrogen gas will have lots of collisions, and so will always emit the pattern of spectral lines shown above. If you see the pattern seen above, then you know the gas is hydrogen. You can identify it from its light.

The figure below shows the spectra from hydrogen and helium compared.



Think of these patterns as “fingerprints.” They are so easy to tell apart that even if the gases hydrogen and helium were mixed, we could tell how much hydrogen and how much helium was present.

These spectral fingerprints were once a mystery. They were only explained through the creation of the theory of quantum physics, the very theory that I just explained to you. Now they are no longer a mystery, but they are an incredibly powerful way to identify elements and molecules. Measurement of spectra such as these has allowed us to determine the gases on the surface of the Sun, and even to measure the gaseous emissions from chemical plants remotely – just by careful measurement of the light coming from the gas.

The fact that electrons can only change energy by quantum leaps makes possible one of the most fascinating inventions of the 20<sup>th</sup> century: the laser.

## Laser – a quantum chain reaction

Lasers are used to burn holes in metal, to send information at enormously high rates over fibers, to read supermarket labels, to measure the exact shape of irreplaceable sculptures, to give spectacular light shows, as convenient pointers, to make holograms, and to find the distance to a remote object (including the moon). Future uses may include the triggering of controlled nuclear fusion, and in shooting down military airplanes and ballistic missiles.

Lasers work on the principle of the stimulated quantum leap. The original theory for this phenomenon was made by Einstein, when he calculated that a passing light wave would trigger a quantum leap in an excited atom. In other words, if an atom has extra energy, then one photon would stimulate the atom to emit another photon. The word laser is an acronym for “light amplification by stimulated emission of radiation.” You should learn the words that make up this acronym.

According to Townes, they briefly considered an alternative name: electromagnetic radiation by stimulated emission of radiation, which would make the acronym *eraser*.

If there are many excited atoms present, then the result can be a chain reaction of light. One photon triggers emission of another, and then the two photons trigger another two, and these four trigger four, then eight, sixteen, etc. The reaction stops only when all of the atoms are de-excited. This kind of chain reaction was first achieved experimentally by Charles Townes, now a professor in the Physics Department at Berkeley. His first experiments used microwaves instead of visible light, and the device was called a “maser.” (The m stands for microwave.) He and Arthur Schawlow figured out how to make them work with visible light, and such lasers were soon built. Lasers now work in the infrared, the ultraviolet, and work has been done to try to get them to work with x-rays. The principle for all these is the same: a photon chain reaction.

As with the nuclear bomb, the chain reaction can happen very quickly. When this occurs, the pulse of light can be extremely powerful, although very short. Such lasers are called pulsed lasers, and they are the most powerful ones. These are the kinds that are being used at our national laboratories in attempts to ignite nuclear fusion without using a fission primary.

However, it is also possible to operate the laser in a continuous manner in which the light output remains constant. (That makes it analogous to the sustained chain reaction in a nuclear reactor.) To do this, we must continuously excite new atoms at the same rate that they are emitting. This is done in a gas laser by sending an electric current continuously through the gas. Continuous lasers are used for laser communications (through fiber optics), for measurement (rangefinding and leveling) and which you see in laser pointers and supermarket label readers.

The laser has two important properties that make it unlike the other chain reactions we studied, and contribute enormously to its value. They are:

- The emitted photons all have identical frequency
- The emitted photons all have identical direction

Identical frequencies means that the light is only one color, i.e. it is monochromatic. This is the feature that makes lasers really valuable for communications. Information is carried by a laser beam by modulating it, i.e. by changing its amplitude. You want the original beam to be as constant as possible. If there are multiple frequencies in the beam, then beats between these frequencies will give a false modulation.

You'll sometimes hear that the light from a laser is *coherent*. Coherent is a fancy word meaning that only one frequency is present – or at least that the range of frequencies present is very small.<sup>1</sup>

The fact that the emitted photons have identical direction is more important than you might guess. It means that the beam comes out of the laser with all the light parallel, well collimated. That's why a laser beam doesn't seem to spread very much, unlike a flashlight beam or headlight of a car. Even sunlight has light coming from different directions: since the sun covers about one angular degree in the sky, light from different parts comes at slightly different directions. But laser beams are different. Theoretically they should spread a little, since they are waves. But that spreading angle can be tiny, since the wavelength is so short.<sup>2</sup> Sometimes it is necessary to spread a laser beam, for example, if you want it to illuminate a hologram. You can do this by passing it through a lens or bouncing it off a curved surface. But the light originally produced is very well collimated.

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<sup>1</sup> Optional: the "coherence time" is equal to one divided by the bandwidth, i.e. the difference in the maximum frequency present minus the minimum. If the bandwidth is small, then the coherence time is very long.

<sup>2</sup> The equation for spreading is the one we discussed in chapter 8:  $B = (L/D) R$ . For a beam of diameter  $D = 5 \text{ mm} = 5 \times 10^{-3} \text{ meters}$ , and  $L = 0.5 \text{ microns} = 5 \times 10^{-7} \text{ meters}$ , the  $(L/D) = 10^{-4}$ . So in  $R = 100 \text{ meters}$ , it will spread only 1 cm. In 1 km, it will spread to a size of 10 cm. If you see a laser light show, by the time the end of the beam is 1 km away, it still looks pretty small.

## **laser measurements**

The collimation of the narrow laser beam makes them useful for measurement that otherwise might be difficult. A pulsed laser beam can be directed at a distance object, and the bright spot on the object can be observed in a telescope and have its time to return accurately measured. That time then gives the distance to the object. That is the basis for laser rangefinding. If you measure distance for many different directions, you get a record of the entire shape of an object. Lasers have been used in this way to measure the changing shape of volcanoes, the interiors of buildings and caves, and historic structures such as the Roman Coliseum. Laser scanners, based on similar principles, are now being used for very detailed measurements of the shapes of objects, including valuable and irreplaceable sculptures.

At construction sites, a laser beam can be made level, and that beam then placed across the entire construction site to make the structures level with each other. Lasers are sometimes lined up with boundaries of property, to see what objects are in the property and which are outside. They are particularly useful for hilly land where the surveyor could not lay out a string. They can be used to show construction workers exactly where to lay foundations or columns.

An intriguing use of lasers for measurement was done for the movie “The Two Towers” (part of the Lord of the Rings trilogy). An actor (Andy Serkis) climbed down cliffs, walked on all fours, moved in complex ways – and the positions of his shoulders, head, hands, and other parts of his body were measured using lasers to detect corner reflectors that had been attached to them. A computer then generated a new image, completely computer-generated, of an imaginary creature named Gollum.

## **supermarket lasers for bar-code reading**

Supermarket lasers emit a very narrow, monochromatic laser beam, and they scan this in a complex pattern. In addition to the laser, there is a detector that looks at reflected light. The detector is designed to measure only light that matches the frequency of the laser. (They use a filter to eliminate all other light.)

When the beam scans across the bar code on the product, the reflected light blinks rapidly, matching the dark and light spots on the code. The detector notices this rapid blinking, and checks the pattern. From the pattern, it can look up the price in a catalogue, or just record the fact that the item was purchased. The narrowness of the laser beam is important for being able to record the narrow pattern.

It turns out that the easiest way to point the laser beam is not by moving the laser, but by bouncing it off a spinning hologram. Different parts of the hologram point the beam in different directions.

## **laser cleaning**

Lasers are being used to clean old and valuable statues, without damaging the surface. To do this, they take advantage of their ability to deliver high power for very short pulses. A laser pulse delivered to the surface can cause very intense heating, enough to vaporize soot and oil, but if the pulse is very short (typically a laser is used with a pulse that lasts only a few nanoseconds), then it is only a very thin layer of the statue that is heated. The image below shows a statue that was cleaned in this manner.



Ancient sculpture, before and after laser cleaning  
(image borrowed from [www.buildingconservation.com/articles/laser/laser.htm](http://www.buildingconservation.com/articles/laser/laser.htm))

Needless to say, when something is developed for scientific or artistic reasons, someone will figure out how to make money from the process. Laser cleaning and whitening of teeth is already being practiced in the United States, and dentists are looking seriously into the use of lasers for removal of dental caries and other medical procedures.

## **laser weapons**

Ever since the laser was invented, the military has looked for potential weapons applications. Lasers can deliver a lot of energy at the speed of light. This application was limited, at first, by the size of very energetic lasers. But recent development of portable (can be carried on airplanes) lasers using carbon-dioxide have revived interest. Lasers have been used to shoot down drones – small, unmanned aircraft. Lasers are frequently mentioned for their possible application for shooting down missiles. This is a situation in which speed is needed, since the missiles travel fast.

The laser beam does its damage by depositing heat on the surface. If the surface is moving, then the laser beam must follow the same spot. A potential problem with such systems is that laser beams can be reflected. If the target is made reflective, then little light is absorbed.

A more serious application for the military is as an anti-satellite weapon. A laser can deliver a substantial amount of energy to a satellite over a period of a few minutes, and the satellite has no way to lose that energy except by heating up and radiating it. Of course, most satellites would be damaged by the heating.

## **Laser eye safety**

Lasers can be dangerous to eyes for several reasons. The simplest, of course, is that they have high power that can be concentrated on a small spot, and the eye is delicate. But there are other reasons. The light from lasers is frequently very highly collimated, and parallel light is focused by the eye on the retina of the eye. Even relatively weak laser light can become intense when focused on the retina. If the laser light is in the infrared or some other invisible wavelength, then the victim may not even know his eye is being damaged. For these reasons, people who work in or visit laser laboratories are usually required to wear special goggles that block out all light of the laser frequency, while allowing other light through.

## **laser eye surgery**

Lasers have found an important use in surgery, particular for the eye. A broad laser beam can enter the eye, and be focused on a tiny spot. Because the power of the beam is spread out everywhere except at the focus, there is not much heating except at the target spot. Perhaps the most exciting application of this technique is to “weld” a detached retina to the back surface of the eye. This procedure is now common, and it has prevented thousands of people from going blind.

Lasers are also used to cut away parts of the cornea, to reshape it so that it focuses better on the retina. This has given “normal” eyesight to people who otherwise would have to wear glasses or contact lenses. Such surgery can be done in a few minutes in a doctor’s office. Of course, this kind of surgery is not able to cure the loss of accommodation that occurs with age. The most popular kind of this surgery is called “Lasik” for laser-assisted in-situ keratomileusis. In this procedure, knife is used to open a flap on the cornea, and then a laser is used to vaporize and remove portions of the underlying cornea. the flap is put back in place, and the patient walks out of the doctor’s office. The patient can see immediately. The eye takes several days for its initial healing, and is not completely normal for several months.

Lasers are also used for other kinds of eye surgery. One of these is to stop the bleeding of blood vessels in the retina that lead to macular degeneration. The heat from the laser, delivered precisely to the blood vessel, can cause the blood to clot and seal the leak. (The effect on the blood is called laser photocoagulation.)

Lasers are also being tried for other types of surgery. The highly focused beam can cut a very small region, and the heat automatically cauterizes the cut flesh (i.e. stops it from



bleeding). Moreover, there is no need to sterilize a laser beam, in the way that people have to sterilize knives.

## Solar cells and digital cameras

When light hits a solar cell, each photon has enough energy to knock an electron out of an atom. When it does this, the liberated electron can be used to create an electric current. This is the basis of the operation of solar cells. They turn the energy of sunlight into electric current.

Solar cells may very well become a major source of electric power in the future. Present day solar cells produce power at about three times the cost of power from natural gas, oil, or coal. An economist might say that this estimate is true only if you don't include environmental costs, such as the damage done to the environment and possible global warming. If you include those cost in, then solar cells may already be cheaper than fossil fuels.

The future of solar cells can become brighter if their cost can be brought down, or if the cost of fossil fuels increases significantly. A promising technology for cheap solar cells uses *amorphous* silicon; check the web for details.

Digital cameras work in exactly the same way as solar cells: they turn photons into electricity. In a digital camera there is one photocell for each pixel, i.e. for each picture element. A 6 megapixel camera has 6 million of these photocells. Each one gives an electric current that can be read by the small computer that is part of every digital camera.

Some of the first digital cameras ever used were aboard United States spy satellites. They could take the image and use radio signals to send the image back down to the ground. At that time, the fact that this could be done was highly classified.

## Photon energy and color

One of the most surprising results of quantum mechanics is the fact that the energy of a photon does not depend on the intensity of the light beam. A more intense beam contains more photons, but none of the photons are more energetic.

But equally surprising (at least to the early scientists) was the fact that the absorbed energy does depend on the frequency of the light! We now interpret this to mean the energy of the photon depends on the frequency, i.e. on the color of the light. The equation relating the two was postulated by Einstein:

$$E = hf$$

where  $E$  is the photon energy,  $f$  is the frequency, and  $h$  is a famous and important number called “Planck’s constant.” If  $f$  is in Hertz, and  $E$  is in joules, then the value of  $h = 6.6 \times 10^{-34}$ . If you want the energy in electron volts, then use  $h = 4 \times 10^{-15}$ .

Let’s use this value to calculate the photon energy for green light ( $f = 6 \times 10^{14}$  Hz) That gives the energy to be:

$$E = hf = (4 \times 10^{-15})(6 \times 10^{14}) = 2.4 \text{ eV}$$

Does this result surprise you? Remember that one eV was the approximate energy of electrons in atoms. This shows that photons of visible light has about the same energy. Of course, blue photons will have slightly more energy (since they have higher frequency) and red photons will have slightly less energy.

This means that visible light photons have enough energy to affect many atoms and molecules. In particular, they have enough energy to knock an electron out of an atom. This is why visible light can produce electric current from solar cells.

## image intensifiers

The human eye cannot see the light from a single photon. An electronic device that amplifies the light from a single photon, allowing humans to see it, is the “image intensifier.” It works on a principle very similar to that in photocells – using a photon to create an electric current. But in an image intensifier, the light hits metal rather than a crystal.

A modern image intensifier consists of a large number of narrow tubes, tightly packed together in a configuration called a “multichannel plate.” When a photon enters the end of one of the thin tubes, it typically hits the wall of the tube before going very far. Visible photons, even in very dim light, have an energy of 2.4 eV, and that is enough to knock an electron off the surface. (This is called the “photoelectric effect”, and it is what inspired Einstein to create his photon equation.) An electric field accelerates the electron down the tube, and it soon crashes into the side, and knocks out additional electrons. This process continues as an avalanche, and by the time all the electrons reach the end of the tube, the electron signal can be very large. These electrons hit a phosphor, and make a bright spot.

The entire stack of tubes can be placed at the back of a camera. The photons hit the multichannel plate instead of film, and they trigger the electron avalanche that eventually emerges from the end of the tube hits a piece of glass coated with a phosphor. If a photon entered the front end of the stack, then there will be a bright spot at the other end – bright enough for a human to see. Multichannel plates are used in most of the inexpensive image intensifiers that can be purchased on the web.

## **Xerox™ machines and laser printers**

The Xerox machine (the generic term is “photocopier”) takes advantage of the unusual properties of the element selenium. If you put charge on a selenium surface, the charge stays there. However, if you shine light on a region of the selenium surface, the energy of the absorbed photons is sufficient to eject the charge. But unlike metals, selenium is *not* a good conductor of electricity, so only the region that was hit by light loses its charge.

If the selenium is then exposed to a cloud of carbon soot, the soot will be attracted to the charged regions. The result is that every where that light hit the surface stays clean, and all the places where no light hit, get sooty.

Once the sooty selenium is ready, a piece a paper is brought into contact with it, and it picks up the carbon. That dirty paper becomes the Xerox copy. The soot contains a binding material, and when the paper is heated (on the way out of the machine) the soot is permanently bound to the surface.

If the paper gets stuck before it is heated, and you have to open the machine to extract it, you’ll find that the soot doesn’t stick, and your hands and anything else that touches the paper become dirty.

A laser printer is a Xerox machine in which a laser is used to expose the selenium instead of an optical image. The laser scans across the surface with a fine beam whose brightness varies in just the way needed to produce the image.

## **Compact disks and DVDs**

CDs and DVDs make use of the fact that a laser beam can be focused to a small spot. The compact disk has music recorded on a thin layer of aluminum buried inside the plastic. The music has been recorded with small bumps and “lands” between the bumps, about 0.5 microns wide and about 1 micron long. Each spot represents a 0 or a 1, and the reflected intensity is measured to read the pattern. The light shines on only one bit at a time. The CD is spun, about 1.4 million such bits pass the focused laser beam every second. The CD player can distinguish between 0s and 1s from the amount of scattered light that comes back, at this megahertz rate.

Because the laser beam can be focused, it is possible to record even more information on a disk by having several layers on one disk. This method, along with smaller bump size, is used for advanced DVD recording to enable them to record long movies. The outermost layers have to be partially transparent so that some of the light passes through it to the deeper layer. To read the bumps on one of the two layers, the light is focused on it. Any light reaching wrong layer will be out of focus. Because the spot is broad, it takes a longer time for the bumps and lands to pass under it, so the reflected pulses are longer in duration. These longer pulses (from the unwanted layer) can be eliminated by the electronics. DVD players typically have four layers (they look at two from the top

and two from the underside) to store all the information for a movie. Combine that with the smaller bump size, and an advanced DVD can hold seven times as much information as a CD. The first DVD player was marketed in 1997.

## **Gamma rays – and x-rays, again**

Can you guess what the photon energy would be for a gamma ray? Stop for a moment and try. Recall that visible light photons have energy of about 2.4 eV.

Now let's do the calculation. In Chapter 9 (invisible light) we said that the frequency of a typical gamma ray was about  $3 \times 10^{21}$  Hz. Using Einstein's photon energy equation:

$$E = hf = (4 \times 10^{-15})(10^{21}) = 4 \times 10^6 \text{ eV} = 4 \text{ MeV}$$

The appearance of MeV in this result means that gamma ray photons have enough energy to affect a nucleus. Experiments show, for example, that a 4 MeV gamma ray can break a deuterium nucleus into its constituent proton and neutron. Radioactive decays, which release energies typically in the MeV range, often emit gamma rays.

Let's do a similar thing for x-rays. Recall that x-rays are produced when an electron is accelerated to an energy of 20,000 to 100,000 electron volts, and hits a target such as tungsten. According to the Chapter 9 table, typical x-rays have frequencies of about  $10^{19}$  Hz. According the Einstein photon equation, the energy for x-ray photons will be

$$E = hf = (4 \times 10^{-15})(10^{19}) = 40,000 \text{ eV} = 40 \text{ keV}$$

This should not surprise you. It shows that most of the energy of the fast electron goes into the energy of a single x-ray photon.

## **fiber optics communications (again)**

In Chapter 9, we explained that light is an extremely good way to send signals because of its high frequency. (Recall that Shannon's information theorem says that the bits per second is approximately equal to the frequency.) But now we can get an interesting result from quantum mechanics: high frequency isn't enough. We also need high power.

Here is why: a one milliwatt laser beam (typical for a laser pointer) has  $10^{-3}$  joules/sec =  $6 \times 10^{15}$  eV per sec. Since each photon is 2.4 eV, this means that the light has a little over  $2 \times 10^{15}$  photons every second. The frequency for green light is  $6 \times 10^{14}$  Hz. So there are only about 3 photons per cycle, on average.

That is pretty low. Can you see why the communications would not work if the value were less than one photon per cycle? You can not send signals faster than the photon rate, and even three per cycle is pretty low. The value of three is only an average number, and statistical calculations show that if the average is 3, then about 5% of the

time there will be no photons at all in a given cycle, even when the cycle is supposed to have three. That will result in an error. The conclusion is that enough power must be used to avoid this “photon limit.” To avoid high error rates, you need many more than one photon for each cycle.

## Do photons really exist?

We’ve been talking about photons as if they are particles. Yet we know that they are electromagnetic waves. So how can we do that? Do photons really exist? Are they particles, waves, or both?

In fact, if you consider all the phenomena that we have discussed, the “photon nature” of electromagnetic waves manifests itself only when the wave is emitted or absorbed. Of course, that is when we interact with them, so that is important. But in between – after emission and before absorption – the “photon” nature of light doesn’t seem to exist.

If that strikes you as weird, then good. It is weird, and it still bothers many physicists. Let me illustrate what it means with a simple example, the soap bubble.

Recall that the colors of the soap bubble came about because some of the light wave bounced off the inner surface of the bubble, and some bounced off the front surface, and when these two waves came together, the waves interfered. Some colors (the ones that came out in phase with each other) were made stronger, and some (those that cancelled) were made weaker or nonexistent.

How does this interference fit in with the picture of photons? Let’s imagine that we turn down the intensity of the light until only one photon every minute is detected reflecting off the soap bubble. You might think that the photon was reflected off the outer surface of the bubble, or off the inner surface, but obviously it couldn’t have been reflected off both. So at very low levels of light, you would think that all the colors that arise from wave cancellation would disappear.

The experiment has been done, not with soap bubbles, but with mirrors. In fact, it is not hard to do, and can be done by undergraduate physics majors in the upper division laboratory. The results are unambiguous. It is as if the photon split in half, and bounced off both surfaces.

In fact, the best way to think of light is as a wave that can be emitted or absorbed only in quanta – but that in between, it is a wave. It moves like a wave, diffracts like a wave, bends like a wave, and interferes like a wave. But it is not emitted and absorbed like a wave, but like a particle. This is the famous “**wave-particle duality**” of quantum mechanics that mystifies many people.

## Semiconductor Electronics<sup>3</sup>

Essentially all modern electronics is based on quantum physics: the fact that electrons are waves. Their wave nature is very important when they flow through crystals known as semiconductors. (The word semiconductor comes from the fact that the material is not as conductive as a metal, yet it still conducts.) The most important semiconductors are silicon and germanium, often with small amounts of aluminum or phosphorus mixed into their crystals. Important applications of semiconductors include the microprocessor that runs your computer, laser diodes that play your compact disk players, and virtually all other modern electronics in your TV, your car, and even in screw-in fluorescent light bulbs.

The key feature of semiconductors, the one that makes it so important, is the fact that not all energies of electrons can flow. There is an energy gap (typically about an electron volt) just as there is in the hydrogen and helium atom. This energy gap is a result of the fact that electrons are waves. When electrons move through crystals, and their wavelength happens to match the crystal spacing, then there is a very strong reflectance that results in an energy gap. As with a hydrogen atom, the typical energy gap is a few electron volts.

Light emitting diodes and semiconductor lasers both take advantage of this energy gap to emit photons.

### Light emitting diodes (LEDs)

Light emitting diode (LEDs) is a semiconductor that emits light when a voltage is applied across it. Those little red lights that let you know your computer (or anything else) is on is usually an LED. The large TV displays used at stadiums and for some street displays are large arrays of red, blue, and green LEDs. LEDs light up your watch when you push the button. Many traffic lights are being replaced by LEDs because the LEDs are more efficient (they don't produce waste heat) and they don't burn out like tungsten filaments. In the near future, most flashlights will use LEDs instead of small tungsten bulbs. (Expensive flashlights already use them.) Infrared LEDs on your TV remote control send a burst of invisible light to the TV to tell it to turn on, off, or to change the channel.

An LED works in a simple way: an applied electric voltage gives an electron extra energy.<sup>4</sup> Because of the energy gap, it can't lose little bits of this energy, but only the

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<sup>3</sup> Note for the experts: Most introductions to semiconductors emphasize the importance both of electrons and of objects call "holes" – bubbles in the electron sea, i.e. the absence of electrons. Holes behave much like positively-charged electrons. Although holes are important for semiconductor engineering, all of the key quantum-mechanics issues can be discussed without introducing them. They should be the first topic for students who want to go deeper into semiconductor physics than we do in this chapter.

entire amount, all at once. It does this by emitting a photon. The color of the photon is related to the energy gap by the Einstein formula  $E = hf$ . An LED with a small energy gap gives red light; an LED with a large energy gap gives blue light.

### Diode lasers

A diode laser is the kind that is used in supermarket scanners, in laser pointers, and in CD and DVD players. It is very similar to an LED: it is a small semiconductor in which the electron is “excited” from its low energy to a higher one. The main difference between a LED and a diode laser is that the diode laser takes advantage of stimulated emission, i.e. the fact that one emitted photon can stimulate the emission of another photon. (To achieve this required devising a semiconductor in which the photon would not be emitted spontaneously before it could be stimulated to emit.)

Because the diode laser is a laser, it means that the photons that come out are all going in the same direction. This collimation is not quite as good as for a large size laser, but it is much better than in the LED, in which the light comes out in all directions. The collimation allows the light to form a very narrow beam that does not spread, and which can be focused to a very small spot. This is important for most of the applications mentioned above.

### Diodes – to turn AC into DC

One of the earliest (and still the simplest) semiconductor device is the diode rectifier, often called a **diode** for short. The reason this is so important is that almost all electronics requires DC (direct current) in which the electrons only flow one way. Yet, as we discussed in Chapter xx, the electricity that comes to our homes is AC (alternating current). A diode can turn AC to DC by letting through only the half of the current that is flowing in the right way.

To make a diode you put two semiconductors that have different energy gaps into contact with each other.<sup>5</sup> As soon as that is done, electrons begin to flow from the one which has higher energy to the one that has lower energy. It is just like balls rolling down a hill. The flow finally stops when enough electric charge builds up to repel additional electrons. The same thing would happen with balls rolling down a hill: if they were charged, eventually the repulsion would keep other balls from rolling down.

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<sup>4</sup> Most books will describe in detail how energy is delivered to the electron. It usually involves a junction between two semiconductors that have different “doping” which leads to different energy levels. But the key reason that light is emitted is because of the energy gap.

<sup>5</sup> For the experts only: The two materials are often both made out of silicon, but they have different impurities purposely mixed in, for example, aluminum in one and phosphorus in the other. This creates “donor levels” and it is the energy gap between these donor levels that plays the key role. Diffusion of charge carriers brings these donor levels to the same energy, and that diffusion creates the electric field at the junction.

The electrons that have accumulated create a strong electric field near the junction. This field prevents current from flowing. If you weaken this field by applying an extra voltage (e.g. from a battery) then additional electrons will flow to rebuild it. But if you strengthen the field by applying an additional voltage in the same direction, then no current can flow. This is the basic idea behind the semiconductor diode. It lets current flow one way, but not the other. Put AC into it, and the current will still flow just one way. That's the way it turns AC into DC. (The magnitude of the DC will still vary with time, going up and down, but it will never go the other way. To smooth it out takes other electronics.)

Diodes have a long history. Like superconductors, they were used before they were understood. One of the earliest diodes ever used was the “cat’s whisker” of the old crystal radio sets that amateurs (and even the author of this book) used to make as a hobby. A thin wire was delicately placed on a crystal and moved around until a spot was found that conducted electricity in just one direction. The wire was supposed to be as thin as a cat’s whisker – so these were called cat’s whisker diodes. Below is a cartoon from 1923 depicting an amateur radio builder trying to get his cat to move his whisker to just the right place on the crystal.



(found on the web site <http://electronics.howstuffworks.com>)

But real cat’s whiskers were never used.

## Transistor amplifiers

Stereo sets, TVs, CD players, all contain transistor amplifiers – circuits based on quantum physics that are used to make signals stronger. Modified transistor amplifiers become transistor switches, and that is the fundamental element used in modern computers. The transistor has become so important in our lives that it is a serious candidate for the most important invention of the 20<sup>th</sup> century. (Of course, it is competing with the airplane, antibiotics, wireless communication ....)

To explain these things, we begin with the concept of an amplifier.



## amplifiers

An amplifier is a device that make an electric signal stronger. Doesn't doing that violate the conservation of energy? No, because all amplifiers require an additional power source, usually a battery or a connection to a wall plug.

What amplifiers really do is use a small signal to control a much larger one. Amplifiers are really valves, devices that change a large current to make it vary with time in the same pattern as does the small controlling voltage. Think about a water valve. You move a handle a small amount, and that can controls and modulate a strong stream of water from a hose or faucet. You expend very little energy in doing this, but the changes in current can be huge. In a similar manner, the small voltage (for example, from an antenna) can control the large currents that flow to a loudspeaker. If the control is precise, then the sound from the loudspeaker can be an exact replica of the shape of the small electric signal controlling it. That's what an amplifier does.

The first electronic amplifiers were vacuum tubes. In fact, such tubes were once called electronic *valves*, and in England, they still are. Vacuum tubes were based on the fact that electricity flowing through a vacuum could be changed by the small voltage.<sup>6</sup> (The vacuum was located inside a glass tube, and that's the origin of the term *vacuum tube*.)

Vacuum tube amplifiers could also be used as electric switches, devices in which a small signal can turn a large current completely on or off. Such a switch is really just a very strong amplifier. The reason that switches are so important is that they are the fundamental electronic circuit of the computer. All of the computations done in computers are done by switching electric currents.

Very few electronics still use vacuum tubes; about the last tube remaining in use is the very large picture tube used for some TV sets. Vacuum tubes have been almost completely replaced by a semiconductor amplifier known as a transistor.

## transistors

The transistor is a device built out of a semiconductor material (such as silicon or copper oxide) that acts as an amplifier or as a switch. Transistors are far more reliable, much faster, they take less power, and they generate less waste heat. They were invented in 1947.<sup>7</sup> In the 1960s, portable radios commonly contained 8 transistors, and were called

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<sup>6</sup> In the vacuum of the tube a tungsten filament heated a piece of metal called a cathode that emits electrons when it was hot. The electrons would flow through the vacuum to another piece of metal called an anode. In between was a grid of wires. Small voltages applied to this grid could make large changes in the current flowing through the grid. This design is still used in CRT (cathode-ray tubes) displays.

<sup>7</sup> In 1956 the Nobel Prize in physics was awarded to W. Shockley, J. Bardeen, and W. Brattain of Bell Telephone Laboratories for their invention of the transistor.

“transistor radios.” (We now often call transistor radios simply “transistors” – but it is useful to know that the original transistor was the electronic component, not the whole radio.<sup>8</sup>)

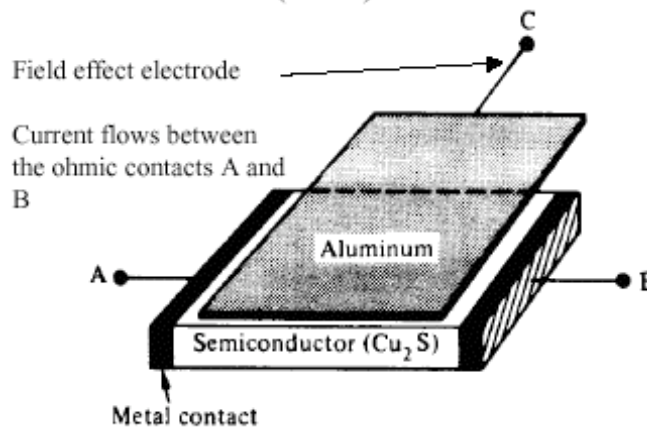
The size and cost of transistors has continued to decrease ever since. An important breakthrough came when engineers figured out how to put many transistors (along with wires and charge storage devices) on a single chip of silicon – creating a device called the “integrated circuit.” The Nobel Prize in 2000 was awarded for this invention.

The integrated circuit really made Moore’s Law start to operate (see Chapter 5). As the transistors were made smaller, the complexity of circuits could grow. The first full microprocessor (computer that has all of its complex circuitry on one chip of silicon) was created in 1971. Now we have over ten million of the quantum devices called transistors on a single chip of silicon.

### Optional: How the transistor works

Because of the importance of transistors, there has been a huge development of the technology, and many different kinds have been created. I’ll describe one of the simpler, but also one of the commoner types of transistors – an FET (which stands for “field effect transistor”). A variation of this is called a MOSFET (for metal-oxide-semiconductor FET). If you look up these terms on the web, you’ll get lots of references.

In a FET, a current normally flows along a narrow semiconductor “channel.” In the diagram below, the semiconductor is a compound of copper (Cu) and sulfur (S).



The current normally flows from A to B. But a small voltage on the aluminum cover C can make big changes in that current. Here’s why it works: Remember that when we put

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<sup>8</sup> Other terms that have been similarly shortened include microwave (the original was microwave oven), watch (short for wrist watch), piano (short for piano-forte), the vacuum (short for vacuum cleaner), Frankenstein (short for Frankenstein’s monster). Can you think of more?

two semiconductors together, if they had different energy gaps then the electrons tended to flow to the one with lower energy. The same thing happens if you put some positive charge next to the semiconductor, on the piece of aluminum labeled “C” in the diagram. When that is done, then electrons are drawn to the metal and they cross over; as a result, there are fewer electrons in the semiconductor, and that decreases the current that flows from A to B. In other words, a small voltage on the aluminum *depletes* the semiconductor of its conducting electrons, and that affects the current flowing through that semiconductor.

Another diagram of a semiconductor switch in use is shown below.

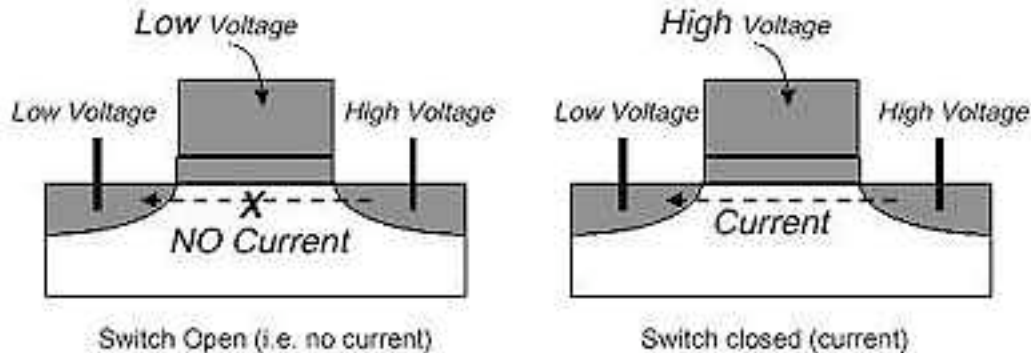


image borrowed from <http://www.sysopt.com/articles/soi/index2.html>

## The physics of superconductors

When we talked about superconductors, we never explained why the electrons can move through the superconducting metal with no loss of energy. In fact, superconductivity was discovered by Omnes in 1911 (he was awarded the Nobel Prize in 1913) and yet the phenomenon was not understood by him or anyone else for many decades. For much of the 20<sup>th</sup> century it was the outstanding failure of the quantum theory that nobody could figure out why superconductors were superconductors!

The reason did turn out to be quantum mechanical, and just as with spectral fingerprints and semiconductors, the answer was the existence of an energy gap. Just as in the other materials, the behavior of superconductors comes about because electrons are waves, and in certain crystals this can lead to an energy gap. Because there is a gap, the energy of the electron cannot change by small amounts. That means it can't lose energy gradually, from many small collisions. The remarkable feature is that because it can't lose energy – it doesn't! So the electrons will continue to flow without energy loss. That's what superconductivity is.

Not all metals behave this way. We now understand that for a metal to become superconductor, an interesting thing must happen: the electrons have to move in pairs. This happens when slow moving electrons pull the positive charges of the metal close to them, and that distortion of the metal tends to attract another electron. The net result is

that electrons attract other electrons. The electrons never get very close, and it doesn't take very much energy to break them apart. That's why this happens only at low temperatures. The two electrons are called "**Cooper pairs**" after the name of the physicist who first predicted their existence.

The full quantum theory of superconductivity was worked out in 1957 by John Bardeen, Leon Cooper, and Robert Schrieffer. They were awarded the Nobel Prize for this work in 1972. They were able to show that the allowed energies of the paired particles were quantized. Cooper pairs could move together at a low velocity, but you could not have them move slower or faster, except by a quantized amount. As strange as it seems, that was the calculation that finally explained the mystery of superconductivity! With an energy gap, the Cooper pairs couldn't lose little bits of energy. And as a result (and this is the really weird part of quantum physics) if the electron can't lose the energy, the collision doesn't take place. The energy gap prevents the collisions that cause resistance. The energy gap is only 0.001 eV – but that is enough to give zero resistance. The superconductivity goes away at high temperature because the Cooper pairs break up.

Despite the fact that we understand superconductivity at low temperatures, once again, superconductivity has a mystery. This time, it is high-temperature superconductors, the ones that become superconducting at temperatures up to 150 K. The BCS theory does not predict their existence, and nobody has been able to figure out why these compounds become superconductors at such high temperatures. We do know that the flow involves Cooper pairs.

## The electron microscope

Objects that are less than a micron in size cannot be resolved with ordinary light because you cannot focus a beam on a spot smaller than the beam's wavelength. If you want to look at something smaller than that, you need a wave with a shorter wavelength. X-rays are sometimes used, but x-rays tend to go right through objects, especially objects that are only a few microns thick. A more widely used option: use electrons. Electron beams with an energy of 50 keV have a wavelength smaller than the size of atoms<sup>9</sup>.

There are several kinds of electron microscope, but the most interesting one is the "scanning electron microscope" or SEM. In an SEM, a beam of electrons is scanned across the object, much as a beam of electrons scans on the surface of a material, and the number which bounce off in a particular direction is measured. The images that we get from an SEM look remarkably like ordinary photos. That's probably because shadows make it look realistic. (The shadows are there because electron beams hitting the back

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<sup>9</sup> Optional: Since electrons have mass, according to the theory of quantum physics (not all of which we have discussed) the wavelength  $L$  has to be calculated from the "deBroglie equation"  $L = h/(mv)$ . The momentum  $mv$  can be calculated if you know the energy  $E = 1/2 m v^2 = (mv)^2/(2m)$ .

side of an object reflect away from the detector, and fewer of them are collected.) Below is an SEM image of the claw of a spider.



Image of a spider claw (black widow) taken with a scanning electron microscope  
(from <http://www.mos.org/sln/sem/widow.html>)

## Are water waves quantized?

Light waves are quantized. Electron waves are quantized. Do you think that water waves are also quantized? Are there only certain allowed energies that a water wave can have? What do you think?

The surprising answer is: yes. How can that be? Why don't we notice?

Let's look at a typical water wave. It might have a frequency of  $f = 1$  cycle per second, (Such a wave has a wavelength of about 1.6 meters.) The energy will be quantized by the Einstein equation  $E = hf = 6.6 \times 10^{-34}$  joules. That is tiny. If a wave hits you, and delivers an energy of one joule, then that consists of  $1/(6.6 \times 10^{-34}) = 1.5 \times 10^{33}$  quanta. With that many wave quanta, the fact that the energy is quantized is impossible to notice. This is a case in which a "quantum leap" is very tiny indeed.

In fact, the quanta are so small that they have never been observed for water waves. They don't even have a name. (Waterons? Hydrolons?) But according to quantum theory, they are there.

A similar quantization happens for all those waves that appear to us as real waves: sound waves, low frequency radio and TV waves, rope and slinky waves. They are quantized, but in the limit of low frequencies, the quanta are so small that we would never notice.

## Uncertainty in quantum physics

We have discussed the wave particle “duality” of quantum physics. The electron, the proton, and even light – have in common the fact that they move like waves, and are detected like particles. The fact that an electron moves like a wave led to its quantum behavior: the fact that only certain energies are allowed in atoms and in semiconductors.

Waves often appear in short bursts we call wave packets. A shout consists of a packet of waves that last for a short time. Splash water with a rock, and a ring of waves moves out. The ring is not very thick, perhaps only a few inches wide. The same is usually true for a quantum wave. It is spread out over a finite distance.

But if an electron is spread out as a wave, where is it, really? When the electron is finally detected (such as when it hits an atom), it will have a definite position. How is that related to the width of the wave?

According to quantum physics, the particle quantum will appear somewhere within the width of the wave, but that is all we can say. Not only do we not know where in the wave it will be detected, but that position is fundamentally not knowable. Just as we could not know exactly when a radioactive nucleus would decay, likewise we can not know exactly where an electron will be found. This is at the heart of the uncertainty principle of quantum mechanics.

Of course, waves don’t have to be spread out very much. If you make a short wave packet, then the particle will always be found within that packet.

### **optional: the precise statement of the uncertainty principle**

You can make the position of a particle certain by making a very small wave packet. But in quantum mechanics, such a wave will break up into many different waves traveling at different velocities. Yet only one particle is present. So once you detect the particle, all the other waves have to suddenly disappear. This sudden disappearance has a special name in quantum physics: it is called “the collapse of the wave function.”

So although the position of the electron may be well known, the velocity is uncertain. That means its energy is uncertain too. These relations are at the heart of the famous *Heisenberg uncertainty principle*. It says if you create an electron with very well-defined position, so that it is known to an accuracy  $\Delta x$ , then the velocity is uncertain by an amount at least equal to:

$$\Delta v = h/(2\pi m \Delta x)$$

(In this equation,  $m$  is the mass of the electron, and  $h$  is Planck's constant.) So if you improve your knowledge of the position (i.e. make  $\Delta x$  small by passing the wave through a small hole), that makes the uncertainty in velocity greater.

A similar thing happens with light. Let's talk about knowing the position of the photon in the x-direction, for a beam of light that is traveling in the y-direction. To determine the x position, you let the light wave pass through an opening of width  $D$ . But in doing that, you make the wave spread out, from diffraction. That means that the velocity in the x-direction is no longer certain; part of the wave is moving to the left, and part to the right. When the photon is detected, it could be moving (at least in part) sideways. It turns out that the diffraction equation that we gave in Chapter 8 is also the Heisenberg uncertainty relation – but in the special form that is appropriate for light.

## tunneling

Tunneling is one of the more famous phenomena in quantum physics. It says that particles can travel to places where they appear to violate the conservation of energy. Tunneling is a consequence of the uncertainty principle, in particular, the fact that for a wave packet the energy of a wave is uncertain. The name “tunneling” comes about because, in effect, a particle can go from one side of a hill to the other, even though it doesn't have sufficient energy to get over the hill.

Tunneling is relatively easily to calculate when you know the height and width of the hill. We teach junior physics majors how to calculate it. Like other things in quantum mechanics, calculations gives probabilistic results. You can't say for sure that something will tunnel, but you can calculate the probability that it will tunnel in a given time. We won't do the calculation here, but instead will discuss the consequences of tunneling, and the practical application in the tunnel diode.

## alpha radiation

Remember alpha particle radioactivity, from Chapter 4? It turns out that this kind of radioactivity occurs because of tunneling. The alpha particle is inside the nucleus prior to the decay, but there are forces that prevent it from coming out. According to ordinary physical laws, it doesn't have enough energy to overcome the attraction of the nuclear force. But, thanks to the uncertainty principle, there is some chance that it will tunnel out anyway. Its energy is uncertain, and therefore there is some small chance at any moment that it will have enough energy to escape. Because nobody can calculate when it will come out, but just the likelihood that it will come out in any time period, the decays occur randomly.

(It is worth pointing out that not all radioactivity is due to tunneling. In beta decay, the electron and neutrino are both created at the time of their emission. They are like the

sound waves that you create when you speak; they didn't exist until they are created at the moment of decay, but when they are created, they can carry away energy. Likewise, x-ray and gamma ray radioactivity is not an example of tunneling.)

So every time you see an alpha decay, you know that tunneling has taken place. Energy conservation was violated, but only for a short period of time. Once the alpha particle is out, the energy it has is identical to the energy it had inside the nucleus. We never actually see it violate energy conservation. We just calculate that it must have done so, but only for a very short period of time. So, in the end, energy is conserved. There is no more energy than there was before the decay. Somehow the alpha particle snuck through. We say that it tunneled.

### **tunnel diodes**

One of the more practical uses of tunneling is a kind of semiconductor amplifier known as the tunnel diode. The tunnel diode works very much like an ordinary diode, with two semiconductors with different energy gaps put in contact. Electrons move across the junction because of the lower energy gap on the other side, and in doing so they create an electric field that repels other electrons. So far, that is the same as an ordinary semiconductor diode.

In a tunnel diode, that region is made very thin, and a battery voltage placed across the junction almost gives electrons enough energy to get across – but not quite enough. However, thanks to tunneling, some do leak through. In a tunnel diode, impurities are added to the semiconductor to make sure that there are a lot of electrons available for this leakage. The current that gets through is called the tunnel current.

The number that tunnel depends on the electron energy. So, if a varying voltage is added to the battery voltage, then the energy of the electrons changes, and that makes tunneling easier or harder. The effect is very strong, so a little bit of voltage change can make a big current change. That is what makes the device into an amplifier. That's what an amplifier is: something where a small change in voltage can make a large change in current.

Tunnel diodes also respond very rapidly to changes in current, faster than do FETs. By making the voltage changes large enough, the current essentially switches on and off. Because tunneling is such a fast effect, tunnel diodes are among the fastest electronic switches we can make, and thanks to that, they are used when high speed switching is important, for example, when routing signals along the internet.

### **scanning tunneling microscopes (STMs)**

If you put a negative voltage on a piece of metal, you would expect it to repel electrons. So why don't the electrons on the surface of metal go flying off the surface? Recall the van de Graaff generator: the electrons stayed on the metal sphere until something was placed close; then a spark jumped. What was holding the electrons on?



The reason the electrons stayed on the metal surface is that, despite the repulsion from other electrons, they also have a binding to the protons of the atoms. To eject an electron takes a bit of extra energy. That energy can be supplied by a photon hitting the surface; we described that earlier, and when a photon ejects an electron from the surface, the process is called the photoelectric effect.

There is another way to get electrons off the surface without giving them enough energy: tunneling. If you put the metal surface very close to another conductor, then the electrons can tunnel across even if they don't have enough energy. This is the principle behind the scanning tunneling microscope. The goal of this device is to map out the surface of a conductor.

First, it is important to understand the geometry. A metal tip is attached to a piezoelectric crystal – a crystal whose thickness can be adjusted to very high precision by applying a voltage across it (the crystal voltage). In addition, a tip voltage is applied to the metal point. As this point is brought closer to the surface (by adjusting the crystal voltage on the piezoelectric), electrons begin to tunnel across from the tip to the surface. When a certain amount current flows, the tip is brought no closer. Then the tip is moved across the surface, back and forth. It eventually scans across the entire surface. That scanning is the S part of the STM.

Here is the tricky part: the position of the tip is adjusted as much as necessary, in order to keep the tip current constant. That means that the tip is being moved up and down (by changes in the crystal thickness) to keep it a constant distance above the surface. The crystal thickness needed to do this is recorded, and it becomes a record of the height of the surface at every location. The height is scanned out in this way. That record can then be made into a map of the surface height.

The STM is so precise that even the shapes of individual atoms can be mapped out in this way. A scanning tunneling microscope is what was used to make the image of atoms that was shown in the figure of Chapter 4, the one that showed the letters “IBM” written in individual atoms on the surface of a crystal.

The STM was also used to place the xenon atoms there. By moving the tip close, and adjusting the voltage, the atoms could be picked up and put down.

STMs are the best way to get images of atoms, and their positions. Right now, their main use is to study the properties of surfaces, and the way atoms are bound to those surfaces. In the near future, STMs may be used to scan across DNA molecules to read the genetic code. Some people think they may be used to store information by adjusting the positions of individual atoms, but I am guessing that that is unlikely, at least for the next ten years.

## tunneling in the Sun

As we described in Chapter 5, the Sun is powered by nuclear fusion. At high enough temperatures, protons, deuterons, and other positively charged nuclei have enough kinetic energy to overcome their electric repulsion, so that they get close enough that the nuclear force brings them together and they fuse.

However, calculations show that the Sun is not hot enough to bring the nuclei that close. Their thermal energy brings them near each other, but not enough to fuse. Yet they fuse anyway. The reason is tunneling. Once the nuclei get close, there is a high probability that they can tunnel right through the barrier of repulsion (it is completely analogous to pushing a weight up a hill) and get close enough for the fusion to take place. In that sense, essentially all of the energy we have on Earth is produced using tunneling. The same process takes place in all stars.

Tunneling is also important in nuclear fission. Calculations show that the forces holding the two fission fragments together are quite strong, too strong to ever let them break apart. But because the fission fragments behave as quantum-mechanical waves, they can overcome this energy deficiency if they do it fast enough. Without tunneling, we would not have fission and its applications (reactors and bombs).

## quantum computers

Unlike most of the other technologies described in this book, quantum computers don't yet exist. Nobody knows whether they will ever prove practical. Yet there is a great deal of interest in them, and so they are worth mentioning.

All computers use quantum mechanics, in that the energies of the electron flow in semiconductors is quantized. The random memory of a computer is based on the storage of electrons on small pieces of metal on the chip surface. Electric charge is quantized, that is, it is always present in some multiple of the electron charge. But despite all these ways that ordinary computers are “quantized,” none of them are what we mean by quantum computers.

In ordinary computers, charge is stored, and it flows through switches. Every computation consists of changing the stored charge by regulating the flow of electric current. But in a quantum computer, the idea is fundamentally different. All manipulations are done with the electron wave rather than with the current. This can be done by changing the wave with an electric field or some other external force. No particle is measured or stored until the computation is all finished.

By working with the waves themselves, a much greater amount of information can be stored, a very large number of computations can be carried out simultaneously using very simple circuits, and much less energy can be used in computation. In a sense, the quantum computer will take advantage of the uncertainty principle. By being careful not

to detect the electron, the spread out wave can carry more information than the simple presence or absence of the electron. Each electron can, in principle, carry the equivalent many bits of information. They are called quantum bits -- “qubits” for short.

At least that is the theory. As of 2003, some very simple computations have been done using quantum computers (about as hard as adding one plus one). But nobody knows whether quantum computing will ever prove practical for really large and difficult computation. Part of the problem is, of course, that we already have pretty good computers for most pretty hard problems, so the quantum computer has to make a lot of progress before they would be put to use for any practical purpose. For the latest, do a web search on quantum computing.

It is important to recognize that most new technologies never become practical in the way that people who try to look far ahead, sometimes called “futurists,” speculate. For example, in the 1920s, and every decade since, futurists have predicted that ordinary people would soon be driving their own airplanes instead of cars. They predicted that this was such a certainty that it surely would happen by the 1940s. Yet, it hasn’t happened yet. In the 1940s, futurists predicted that we would have robots helping us in our homes, certainly by the 1960s. Yet that hasn’t happened. Other things (like laptop computers) have happened. The future is hard to predict. Quantum computing has lots of obstacles before it can become practical, and some of them are fundamental (such as keeping noise out of the computation). They may never become useful. But they may.

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## Quick review

Electrons, protons, and all other particles are quantum waves, in the same sense that a light wave is a wave. Their particle properties refer to the way they behave when they are detected or measured. The wave nature is most evident in the way these objects move from one place to another. One important consequence of their wave nature is the quantization of energy levels, both in atoms and in crystals.

Lasers depend on the fact that the presence of a photon will trigger “stimulated emission” of another photon, as the electron that had that energy changes energy, and this results in a chain reaction of photons. The emitted photons have the same frequency as the one that stimulated it, as well as the same direction. That means that a laser beam spreads very little, and it can be focused to a small spot, and that means that the energy it delivers can be strongly concentrated. That feature allows it to be used for laser cleaning and for surgery. Laser applications that make use of one or more of its properties include CD and DVD sensors, supermarket scanners, weapons, and laser printers.

The relation between the frequency of the light and the energy of the photon is given by the Einstein relation,  $E = hf$ . X-rays and gamma rays have very large values of photon energy; that’s why they seem to be more like particles than do other electromagnetic waves. Visible light photons hitting a surface can give this much energy to an electron, a process called the photoelectric effect. That can eject it, or give it

enough energy that it can be conducted away. The photoelectric effect is used in solar cells, digital cameras, Xerox machines, and image intensifiers.

Semiconductors such as silicon also have their special properties because of quantum mechanics. Put two different semiconductors together, and if their energy levels are different, then some electrons will flow from one to the other. This can be used to make a semiconductor diode (which lets current flow only one direction, thereby converting AC to DC), or a transistor amplifier. Virtually all modern electronics is based on diodes and transistors. A switch, the basic computation element of computers, is a version of the transistor. Integrated circuits consist of thousands to millions of transistors on one piece of semiconductor.

Superconductors work because at low temperature the electrons form Cooper pairs, and the motion of these pairs has an energy gap that prevents the pairs from losing small amounts of energy from collisions. As a result, they lose none.

Electron microscopes work by focusing a very fine beam on the object that is being observed. They can see things much smaller than can visible light microscopes. That's because the wavelength of an electron is smaller than the wavelength of light.

All waves are quantized, but for low frequency waves (water waves, radio waves, sound waves) the quantum of energy is so small that it is impossible to detect the tiny quantum leaps.

The Heisenberg uncertainty principle is a consequence of the fact that electrons and other "particles" behave as waves. Not only is location uncertain, but so is velocity and energy. Uncertainty in energy allows electrons to "tunnel" through regions that appear to violate the conservation of energy. Such tunneling is responsible for alpha radioactivity. Tunneling finds practical applications in the tunnel diode and in the scanning-tunneling microscope.

Quantum computers make use of the wave nature of particles to store information in qubits. Nobody knows if they will prove practical.

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## Internet research topics

Find images taken with electron microscopes. For each one, either find out what the magnification is, or estimate it by finding the size of the object imaged. Find some objects that have images both from ordinary visible light and from electron microscopy. What can be learned best from each kind of image?

Find commercial applications of lasers other than the ones I described in this chapter.

What is the current status of lasers as weapons? Are any being tested? Are any being deployed? Can you find discussion of their potential use for anti-ballistic-missile systems (ABMs)?

Find applications of spectral lines. Which of the systems you find can be used remotely (e.g. in the open atmosphere) and which require laboratory measurements? Find uses for environmental measurement, industrial measurement, and purely scientific (e.g. determining the composition of stars).

Find out what you can about high-temperature superconductors. Do they involve Cooper pairs? Have they estimated the size of the energy gap? What is the highest temperature that people have obtained? Are scientists optimistic about reaching higher temperatures?

Look up “crystal radio” and “cat’s whisker diode” on the web and see what you can learn about the early days of radio reception, including the use of vacuum tubes as diodes.

What is the current status of quantum computing? What is the most complex calculation that anyone has done? What are the problems that are too difficult for ordinary computers that might be solvable if quantum computers become viable?

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## Essay topics

Lasers have several properties that make them special. Describe what these properties are. For each special property, describe practical applications that take advantage of it.

Quantum physics has properties that seem very strange to someone who doesn’t recognize that particles have wave-like behavior. What behavior of electrons would be impossible to understand based on classical (non-quantum) physics? What behavior of light would be impossible to understand based on the classical theory of light (i.e. light as a wave, not a quantum wave)?

Describe phenomena that depend on the presence of an energy gap.

What methods can be used to identify gases, for example, to tell whether a gas is hydrogen or helium or a mixture? Describe the principles upon which the method is based.

What phenomena can be understood as a consequence of tunneling? What practical applications are there to this behavior?

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## Short questions

Stimulated emission is important for

- ☐ integrated circuits
- ☐ superconductors
- ☐ LEDs
- ☐ lasers

Transistors use semiconductors with different

- ☐ frequencies
- ☐ energy gaps
- ☐ densities
- ☐ wavelengths

Compact disk readers use

- ☐ x-rays
- ☐ lasers
- ☐ LEDs
- ☐ spectra

To tell hydrogen from helium, look at

- ☐ their x-ray emission
- ☐ their visible spectrum
- ☐ the photoelectric effect
- ☐ their amplification

Quanta are not observed from water waves because

- ☐ such waves are not quantized
- ☐ the energy of the quanta are too small
- ☐ water atoms are too small
- ☐ water atoms are too large

Xerox machines make use of

- ☐ the photoelectric effect
- ☐ Cooper pairs
- ☐ stimulated emission
- ☐ a chain reaction

Spectral lines occur because

- ☐ electron energies are quantized